# **Year 3 Learning and Progression Steps for Mathematics**

## What are Learning and Progression Steps (LAPS)?

The Learning and Progression Steps are designed to scaffold the learning required in order to meet the expectations of the National Curriculum. Statements in the Lancashire Key Learning for Mathematics document have been broken down into smaller steps to support teachers in planning appropriate learning opportunities. These key pieces of learning will support pupils in becoming fluent in the knowledge and skills of the curriculum and ensure that the learning is effective and sustained.

The number of steps is dependent on the learning and do **not** constitute expectations for the end of each term. The colour coding is **an approximate indicator** of end of term expectations.

Orange (including the end of previous year expectation) are the steps in learning for the autumn term.

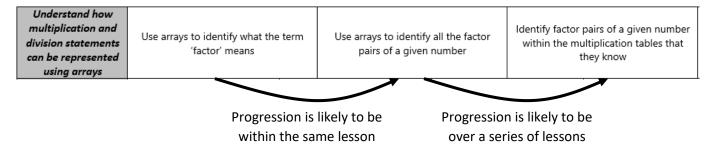
Green are the steps in learning for the spring term.

Yellow are the steps in learning for the summer term and incorporate the end of year expectations.

The colours correspond with the structure of the Lancashire Mathematics Curriculum and reflect how often each learning objective is explicitly taught across the year. Some key learning objectives are not taught in every term, and in some cases not in the summer term. This means that end of year expectations may need to be met before the end of the summer term.

The final step in the progression for each strand of learning is the end of year expectation.

The steps are **not** of equal size and different amounts of time may be required for children to move between individual steps. For example,



Some learning within the same end of year expectation has been split and designed to run concurrently alongside each other. For example,

Read and write numbers up to 1000 in numerals	Read multiples of 1000 to 10 000 in numerals and in words	Read multiples of 100 to 10 000 in numerals and in words	Read numbers to 10 000 where 0 is not used as a place holder	Read numbers to 10 000 where 0 is used as a place holder	Read and write
and in words	Write multiples of 1000 to 10 000 in numerals and in words	Write multiples of 100 to 10 000 in numerals and in words	Write numbers to 10 000 where 0 is not used as a place holder	Write numbers to 10 000 where 0 is used as a place holder	10 000

Some LAPS may need to be completed before another can be started.

### Where have they come from?

The Learning and Progression Steps (LAPS) have been derived from the Lancashire Key Learning in Mathematics statements, identified primarily from the National Curriculum 2014 programmes of study.

## How are they different from the Key Learning Statements?

The Learning and Progression Steps (LAPS) are smaller, progressive steps which support learning towards the Key Learning in Mathematics expectations.

# How are they different from the Key Learning Indicators of Performance (KLIPs)?

The Key Learning Indicators of Performance (KLIPs) document is an assessment tool. The Learning and Progression Steps (LAPS) document is a planning tool and is not intended to be used for summative assessment purposes. However, they may support teachers in judging whether children are on track to meet the end of year expectations at different points throughout the year.

The terms 'entering', 'developing' and 'secure' are used in Lancashire's assessment approach, KLIPs, as summative judgements in relation to age related expectations. Definitions for these terms can be found in the introduction to the KLIPs document.

# How might Learning and Progression Steps (LAPS) in Mathematics be useful?

Learning and Progression Steps (LAPS) may be used in a number of ways. For whole class teaching, LAPS may be used to support differentiation. When planning, it may be appropriate to use LAPS statements to inform learning objectives for a session or number of sessions. Learning and Progression Steps (LAPS) in Mathematics should be selected according to the learning needs of the individual or group. Emphasis however, should always be on developing breadth and depth of learning to ensure skills, knowledge and understanding are sufficiently embedded before moving on.

The LAPS should **not** be used as an assessment tool, but they can inform teachers about children's progress towards the end of year expectations at the end of each term.

### Are LAPS consistent with the other resources from the Lancashire Mathematics Team?

Yes, the LAPS are related to the content of the Mathematics Planning Support Disc and also the Progression Towards Written Calculation Policies and the Progression in Mental Calculation Strategies.

These can be found on the website:

www.lancsngfl.ac.uk/curriculum/primarymaths

# **Key Learning in Mathematics – Year 3**

## Number – number and place value

- Count from 0 in multiples of 4, 8, 50 and 100
- Count up and down in tenths
- Read and write numbers up to 1000 in numerals and in words
- Read and write numbers with one decimal place
- Identify, represent and estimate numbers using different representations (including the number line)
- Recognise the place value of each digit in a three-digit number (hundreds, tens, ones)
- Identify the value of each digit to one decimal place
- Partition numbers in different ways (e.g. 146 = 100+ 40+6 and 146 = 130+16)
- Compare and order numbers up to 1000
- Compare and order numbers with one decimal place
- Find 1, 10 or 100 more or less than a given number
- Round numbers to at least 1000 to the nearest 10 or 100
- Find the effect of multiplying a one- or two-digit number by 10 and 100, identify the value of the digits in the answer
- Describe and extend number sequences involving counting on or back in different steps
- Read Roman numerals from I to XII
- Solve number problems and practical problems involving these ideas

#### **Number – addition and subtraction**

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
- Select a mental strategy appropriate for the numbers involved in the calculation
- Understand and use take away and difference for subtraction, deciding on the most efficient method for the numbers involved, irrespective of context
- Recall/use addition/subtraction facts for 100 (multiples of 5 and 10)
- Derive and use addition and subtraction facts for 100
- Derive and use addition and subtraction facts for multiples of 100 totalling 1000
- · Add and subtract numbers mentally, including:
- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds
- Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction
- Estimate the answer to a calculation and use inverse operations to check answers
- Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction

## **Number – multiplication and division**

- Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
- Understand that division is the inverse of multiplication and vice versa
- Understand how multiplication and division statements can be represented using arrays
- Understand division as sharing and grouping and use each appropriately
- Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables
- Derive and use doubles of all numbers to 100 and corresponding halves
- Derive and use doubles of all multiples of 50 to 500
- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
- Solve problems, including missing number problems, involving multiplication and division (and interpreting remainders), including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

### Number – fractions

- Show practically or pictorially that a fraction is one whole number divided by another (e.g.  $\frac{3}{7}$  can be interpreted as  $3 \div 4$ )
- Understand that finding a fraction of an amount relates to division
- Recognise that tenths arise from dividing objects into 10 equal parts and in dividing one-digit numbers or quantities by 10
- Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators
- Recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators
- Recognise and show, using diagrams, equivalent fractions with small denominators
- Add and subtract fractions with the same denominator within one whole [for example,  $\frac{5}{7} + \frac{1}{\pi} = \frac{6}{1}$ ]
- Compare and order unit fractions, and fractions with the same denominators (including on a number line)
- Count on and back in steps of  $\frac{1}{2}$ ,  $\frac{1}{4}$  and  $\frac{1}{3}$
- Solve problems that involve all of the above

## **Geometry – properties of shapes**

- Draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them
- Recognise angles as a property of shape or a description of a turn
- Identify right angles, recognise that two right angles make a halfturn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle
- Identify horizontal and vertical lines and pairs of perpendicular and parallel lines

# **Geometry – position and direction**

• Describe positions on a square grid labelled with letters and numbers

#### Statistics

- Use sorting diagrams to compare and sort objects, numbers and common 2-D and 3-D shapes and everyday objects
- Interpret and present data using bar charts, pictograms and tables
- Solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables

#### Measures

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)
- Continue to estimate and measure temperature to the nearest degree (°C) using thermometers
- Understand perimeter is a measure of distance around the boundary of a shape
- Measure the perimeter of simple 2-D shapes
- Tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks
- Estimate/read time with increasing accuracy to the nearest minute
- Record/compare time in terms of seconds, minutes, hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon, midnight
- Know the number of seconds in a minute and the number of days in each month, year and leap year
- Compare durations of events [for example to calculate the time taken by particular events or tasks]
- Continue to recognise and use the symbols for pounds (£) and pence (p) and understand that the decimal point separates pounds/pence
- Recognise that ten 10p coins equal £1 and that each coin is  $\frac{1}{10}$  of £1
- Add and subtract amounts of money to give change, using both £ and p in practical contexts
- Solve problems involving money and measures and simple problems involving passage of time

These Learning and Progression Statements (LAPS) are designed to show the necessary steps in learning to make effective and sustainable progress within a single year. They begin with the 'end of year' expectation from the previous year and build up to the 'end of year expectation' of the current year.

The number of steps is dependent on the learning and do **not** constitute expectations for the end of each term.

The steps are **not** of equal size and different amounts of time may be required for children to move between individual steps.

	End of Year 2 expectation				Lea	rning and Progr	ession Stateme	ents				End of Year 3 expectation
	Count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward	Count in steps of 100 from 0 to 1000		Count i	n steps of	50 from 0	Count in s	steps of 4	from 0	Ci	ount in steps of 8 from 0	Count from 0 in multiples of 4, 8, 50 and 100
	Count on and back in steps of $\frac{1}{2}$ and $\frac{1}{4}$	Count up in fractional tenths including where boundaring are crossed, e.g. $\frac{8}{10'}$ , $\frac{9}{10'}$ , $\frac{10}{10'}$ , $\frac{1}{10'}$ , $\frac{1}{10'}$ , $\frac{1}{10}$ , $\frac{1}{10}$	es	including	where boo	tional tenths undaries are 2, $1\frac{9}{10}$ , $1\frac{8}{10}$ etc.	Count up including vare are e.g. 3.6, 3.7, 3	vhere bou e crossed,	ındaries	inc	nt down in decimal tenths cluding where boundaries are crossed, 5.3, 5.2, 5.1, 5, 4.9, 4.8 etc.	Count up and down in tenths
	Read and write numbers to at least 100 in	Read multiples of 100 up to and in word		numerals			000 where 0 is n n the tens colur				to 1000 where 0 is used as a er in the tens column	Read and write numbers up to 1000 in numerals
	numerals and in words	and in words					000 where 0 is n n the tens colur				to 1000 where 0 is used as a er in the tens column	and in words
/alue	No equivalent objective in Year 2			Th	There are no steps towards this end of year expectation						Read and write numbers with one decimal place	
Number and Place Value	Identify, represent and estimate numbers using different representations, including the number line	Identify and represent number to 1000 using concrete mater such as base 10 apparatu	Identify and represent numbers up to 1000 using models such as place value counters, an abacus and arrow cards.			Correctly place multiples of 100 of a number line with multiples of 100 marked but not labelled (with start and end labelled 0 and 100 marked but not labelled 0 and 100 marked		ultiples of elled (with	a number line with multiples of 100 marked but not labelled (with		Identify, represent and estimate numbers using different representations (including the number line)	
Num	Recognise the place value of each digit in a two-digit number (tens, ones)		Make and identify a three-digit number up to equipment such as base 10 app							abacus	and arrow cards	Recognise the place value of each digit in a three- digit number (hundreds, tens, ones)
	No equivalent objective in Year 2	Know that the decimal point separates whole numbers (or tens, hundreds etc.) and decontractions (tenths)	nes,			als to make a ecimal place vs	Use a place va the value o dec		it to one	one o	ify the value of each digit to decimal place in a variety of e.g. the value of the digit 7 in 7 is seven tenths, $\frac{7}{10}$ or 0.7	Identify the value of each digit to one decimal place
	Partition numbers in different ways (e.g. 23 = 20 + 3 and 23 = 10 + 13)	Make a three-digit number using concrete materials, e.g. base 10 apparatus, bundles of straws, place value counters	number base 1 hundre e.g. 6	ition a three r (represent 10 apparatu eds, tens an 543 is 6 hun ) 4 tens (40) ones (3)	ted using us) into nd ones, dreds,	Partition a number (repro- base 10 app hundreds, ten differen e.g. 643 is 1 (500), 14 ten ones	esented using laratus) into las and ones in lat ways, 5 hundreds s (140) and 3	numb apparati in diffe one gro	ion a three-d er using base us into two g erent ways whoup is a multip g. 165 = 150 +	e 10 roups here ole of	Partition a three-digit number without the use of practical equipment into two groups in different ways where one group is a multiple of 10	Partition numbers in different ways (e.g. 146 = 100+40+6 and 146 = 130+16)

Compare and order numbers from 0 up to 100; use <, > and = signs	Compare two numbers up to 1000 when represented using the same concrete materials saying which numbers from 0 up to number is greater or less and use		up to 10 using the s saying whi or less and Pay pa number	three or more numbers 00 when represented ame concrete materials ch numbers are greater use <, > and = correctly. rticular attention to s that have the same e.g. 615 < 652 > 625	Order numbers up to 1 represented using the concrete materials say numbers are greater Pay particular atten numbers that he the same digit e.g. 65, 156 and	ne same ving which or less. ution to ave s,	which num Pay pa nur th	abers up to 1000 saying bers are greater or less. rticular attention to mbers that have ne same digits, 65, 156 and 651	Compare and order numbers up to 1000
No equivalent objective in Year 2	numbers with ones and tenths using concrete materials saying which has more and less and use <, > and = correctly. Pay particular attention to numbers	Order num ones and te concrete saying whice are greate Pay par attention to that ha same of e.g. 6.1, 5.	enths using materials h numbers er or less. ticular o numbers ve the digits,	Compare two or more numbers with tens, ones and tenths using concrete materials saying which has more and less and use <, > and = correctly. Pay particular attention to numbers that have the same digits, e.g. 15.6 and 61.5	Order numbers with tens, ones and tenths saying using concrete materials saying which numbers are greater or less. Pay particular attention to numbers that have the same digits, e.g. 56.1, 15.6 and 61.5	numbe hundreds, and tent which has less and us corr Pay pa attention t that has	wo or more ers with tens, ones hs saying more and e <, > and = ectly. rticular to numbers ave the digits, and 161.5	Order numbers with up to three-digits (hundreds, tens, ones) and tenths saying which numbers are greater or less. Pay particular attention to numbers that have the same digits, e.g. 65.1, 215.6 and 261.5	Compare and order numbers with one decimal place
Find 1 or 10 more or less than a given number	number with up to three-digits, where the tens and hundreds digit stays	Identify th ten more a than a give with up t digits, wi hundreds the s e.g. ten les	nd ten less n number o three- nere the digit stays ame	Identify the number one hundred more and one hundred less than a given number with up to three-digits, e.g. one hundred more than 342	Identify the number one more and one less than a given number with up to three-digits, where the tens digit might change, e.g. one more than 459	ten more a than a give with up digits, whe and hund changes, e	ne number and ten less en number to three- ere the tens dreds digit e.g. ten less a 407	Identify the number one more and one less than a given number with up to three-digits, where the ones, tens and hundreds digits might change, e.g. one more than 499	Find 1, 10 or 100 more or less than a given number
Round numbers to at least 100 to the nearest 10	Identify the multiples immediately before and given three-digit num	d after a	Round numbers with up to three- digits to the nearest ten, e.g. 356 rounds to 360		· · · · · · · · · · · · · · · · · · ·		digits to th	nbers with up to three- e nearest hundred, e.g. 6 rounds to 400	Round numbers to at least 1000 to the nearest 10 or 100

Understand the connection between the 10 multiplication table and place value	Use concrete materials to model the effect of multiplying a one-digit number by 10 e.g. exchange each unit cube for a ten rod and identify what changes and what stays the same	Describe the effect of multiplying a one-digit number by ten, e.g. 7 x 10 =70. The 7 has moved one place to the left; from the ones column to the tens column. A place holder (zero) is needed in the ones column	Use concrete materials to model the effect of multiplying a two-digit number by 10 e.g. exchange each unit cube for a ten rod, and each ten rod for a hundred flat and identify what changes and what stays the same	Describe the effect of multiplying a two-digit number by ten, e.g. 73 x 10 = 730.  Both digits have moved one place to the left.	Use concrete materials to model the effect of multiplying a one- digit number by 100 e.g. exchange each unit cube for a hundred flat and identify what changes and what stays the same	Describe the effect of multiplying a one-digit number by one hundred, e.g. 7 x 100 = 700 The 7 has moved two places to the left; from the ones column to the hundreds column.  Two place holders (zeroes) are needed in the ones and tens columns.	Find the effect of multiplying a one- or two- digit number by 10 and 100, identify the value of the digits in the answer
Describe and extend simple sequences involving counting on or back in different steps	subtraction) in a no calculating the diffe	e the rule (addition or umber sequence by erence between two numbers		uences by using the ied rule	subtraction) in a nu calculating the step size	e the rule (addition or umber sequence by e between non-adjacent ence e.g. 4, □, □, 25, □	Describe and extend number sequences involving counting on or back in different steps
No equivalent objective in Year 2	Know that I represents 1, V represents 5 and X represents 10	Know that in Roman numerals, when a symbol of lesser value is placed after one of greater value the amounts are added e.g. VI is 1 more than 5 which is 6	Know that in Roman numerals a single symbol is not used more than 3 times consecutively*  NB – clock faces occasionally show 4 as IIII	Know how to use the symbols I, V and X to calculate and represent 2, 3, 6, 7, 8, 11 and 12	Know that in Roman numerals, when a symbol of lesser value is placed before one of greater value the lesser amount is subtracted e.g. IX is 1 less than 10 which is 9	Know how to calculate and represent 4 and 9	Read Roman numerals from I to XII
Use place value and number facts to solve problems	See Usin		_	ontexts using the content ent section form the Lanc		ning Disc.	Solve number problems and concrete problems involving these ideas

	End of Year 2 expectation				Learning an	d Prog	ression Stateme	nts		End of Year 3 expectation
	Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting)	The			nt opportunities to sele may differ between cl					Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
		These steps	fit the Lancash	hire Prog	ression Towards Writt	en Cal	culation Policies	and Progression in Me	ental Calculations Policies	
Number – Addition and Subtraction	Select a mental strategy appropriate for the numbers involved in the calculation	Recognise and solve calculations that involve known facts e.g. 60 + 120	Recognise the numbers in accalculations of reordered to calculating the efficient e.g. 50 + 30 becomes the strategy appropriate (This should supported concrete material pictures or joing to the strategy appropriate concrete material pictures or joing the supported concrete material pictures or joing the supported concrete material pictures or joing the supported concrete material pictures or joing the support of the suppor	ddition can be o make more g, 70 + mes 70 nd use where ate dd be dd by terials,	Recognise calculations that require counting on or back mentally e.g. 323 - 70 (counting back in tens) and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	cal re part + 2 str a (T) so	Recognise culations that quire mental itioning e.g. 37 5 and use this rategy where appropriate his should be upported by crete materials, ures or jottings)	Recognise calculations that require counting on mentally to find the difference e.g. 112 – 89 and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	Recognise calculations that require counting on or back mentally, bridging through a multiple of 10 efficiently e.g. 204 – 6 becomes 204 – 4 – 2 and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)  Recognise calculations that require a mental compensation method e.g. 127 + 49 becomes 127 + 50 – 1 and use this strategy where appropriate (This should be supported by concrete materials, pictures or jottings)	Select a mental strategy appropriate for the numbers involved in the calculation
	Understand subtraction as take away and difference (how many more, how many less/fewer)	Use knowledge of nu to 10 to recall the co any two-digit numbe multiple of 10 e.g.	mplement of r to the next		ve the complement of a wo-digit number to 100, e.g. 73 + <b>27</b> = 100		close togeth context sugge away', a cour most effici correctly, e.g. in the field. 93 shearing, h in t Calculated us	t when numbers are ser, even when the ests that it is a 'take nting on strategy is ient and use this. There are 105 sheep a sheep are taken for ow many are left the field? Sing a number line: o 100 then jump of 5 a difference of 12	Recognise and use a counting up strategy when the difference between two numbers can be calculated using three or fewer jumps, e.g. 144 – 86 calculated using a number line:  86 jump of 4 to 90 then jump of 10 to 100 then jump of 44 to 144 gives a difference of 58 or 86 jump of 14 to 100 then jump of 44 to 144 gives a difference of 58	Understand and use take away and difference for subtraction, deciding on the most efficient method for the numbers involved, irrespective of context

Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100	Recall and use addi subtraction facts for multiples of 1 e.g. 60 + □ = 1	100 with 10,	subtract multiples o	and use addition and tion facts for 100 with of 5 using bead strings, a k 10 by 10 grid etc.	Recognise that, when of addition facts to 100, to total 10 and the tens	the two 5s	subtract	and use addition and cion facts for 100 with multiples of 5, .g. 35 + □ = 100	Recall/use addition / subtraction facts for 100 (multiples of 5 and 10)
Recall and use number bonds for multiples of 5 totalling 60 (to support telling time to nearest 5 minutes)	Derive and use addition 100 using bead strings,			Recognise that, when cal 100, the ones total 10	Use add	ition and sub	traction facts for 100	Derive and use addition and subtraction facts for 100	
Recall and use number bonds for multiples of 5 totalling 60 (to support telling time to nearest 5 minutes)	Use related facts to de	erive addition a 100 totall		on facts for multiples of	Use addition and sub	Use addition and subtraction facts for multiples of 100 totalling 1000			Derive and use addition and subtraction facts for multiples of 100 totalling 1000
Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and ones - a two-digit number and tens - two two-digit numbers - adding three one- digit numbers	Add and subtract a three-digit number and ones mentally with no boundaries crossed, e.g. 256 + 3	Add and s three-digi and tens me no boundari e.g. 57	t number entally with ies crossed,	Add and subtract a three-digit number and hundreds mentally, e.g. 375 + 300	Add and subtract a three-digit number and ones mentally, crossing a tens boundary, e.g. 375 + 7	Add and s three-digi and ones crossing a boundary, e	t number mentally, hundreds	Add and subtract a three-digit number and tens mentally crossing a hundreds boundary, e.g. 483 + 30	Add and subtract numbers mentally, including: - a three-digit number and ones - a three-digit number and tens - a three-digit number and hundreds

Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit	Add two numbers with three digits using formal written methods of columnar addition with no exchange from ones into tens, e.g. 326 + 143	Add two number three digits using written metho columnar additio exchange from or tens, e.g. 468 +	formal ds of on with nes into	three digits written m columnar a exchange fro tens and	umbers with using formal nethods of ddition with om ones into tens into	numbe using meth additi from including amou	more than two rs with three digits g formal written nods of columnar on with exchange n ones into tens, g when the 'carried' nt has more than one ten 326 + 147 + 219	Add more than two numbers with up to three digits using formal written methods of columnar addition with exchange from ones into tens and tens into hundreds, e.g. 268 + 34 + 356 using the place value columns to set the calculation out correctly	Add and subtract numbers with up to three digits, using
number and ones - a two-digit number and tens - two two-digit numbers - adding three one- digit numbers	Subtract numbers with three digits using formal written methods of columnar subtraction with no exchange from tens into ones, e.g. 376 – 143	Subtract number three digits using written methor columnar subtract exchange from into ones, e.g. 466 – 22	formal ds of ion with tens	three digits written m columnar sub exchange fr ones and into	tract numbers with e digits using formal ritten methods of nnar subtraction with lange from tens into ones and hundreds into tens, e.g. 426 – 357		act numbers with at numbers of digits three digits, using written methods of ar subtraction with age from tens into and hundreds into s, e.g. 334 – 68 g the place value umns to set the ation out correctly	Subtract numbers using formal written methods of columnar subtraction where the greater number has 0 as a place holder in the tens column with exchange from hundreds into tens then tens into ones, e.g. 304 – 168	formal written methods of columnar addition and subtraction
Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	Use rounding to estimate the be estin	e answer to a calculati nated as 400 + 400 = 8		on, e.g. 423 + 389 could  Use inverse to checked by car				tion, e.g. 423 + 389 = 812 can lowing calculations correctly: 389	Estimate the answer to a calculation and use inverse operations to check answers
Solve problems with addition and subtraction including with missing numbers: - using concrete objects and pictorial representations, including those involving numbers, quantities and measures - applying their increasing knowledge of mental and written methods	Represent and solve a p concrete mate		Repres	ent and solve a representation the co				ve a problem using structured tations such as the bar model	Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction

	End of Year 2 expectation				Lea	rning and Progr	ession Stateme	nts				End of Year 3 expectation
	No equivalent objective in Year 2						ropriate strategi as it will be bas					Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
	No equivalent objective in Year 2	Use concrete mat			e.g. if 8	x 5 = 40  then  4	$0 \div 5 = 8 \text{ and } 40$	÷ 8 = 5				Understand that division is the inverse of multiplication and vice versa
Division	Understand multiplication as repeated addition and arrays	•	ts for the 3 multiplication table     division tacts for the 4 multiplication table     division tacts for the 8 multiplication table								Understand how multiplication and division statements can be represented using arrays	
Number – Multiplication and Division	Understand division as sharing and grouping and that a division calculation can have a remainder	Understand divisio	Understand division as sharing, e.g. recognise contexts that relate to sharing a quantity equally between a given number of groups									Understand division as sharing and grouping and use each
Multipli		Understand division as gr	Understand division as grouping, e.g. recognise contexts that relate to finding how many groups of a particular size there are in a given amount.									appropriately
Number – I	Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers	Recall and use multiplication and division facts for the 3 multiplication table	t	the 4 multiplic table from the ultiplication ta	9	facts for the			the 8 multiplication Recall and use multiplication and division lable facts for the 8 times table			Recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables
	Recall and use doubles of all numbers to 10 and corresponding halves Derive and use doubles of simple two-digit numbers (numbers in which the ones total less than 10)	Use partitioning to derive dou of all numbers to 50 e.g. double 38 becomes double double 8 which is 60 + 16 = 1	of all numbers to 50 ouble 38 becomes double 30 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 60 +  double 60 + double 7 which is 120 +  double 60 + double 60 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 7 which is 120 +  double 60 + double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  double 60 +  doub									Derive and use doubles of all numbers to 100 and corresponding halves

Derive and use doubles of simple two-digit numbers (numbers in which the ones total less than 10)	Use known facts to derive doub e.g. double	les of all mult e 200 is 400	iples of 100 to 500,			erive doubles of all multiples of 50 to ble 150 is 300	Derive and use doubles of all multiples of 50 to 500
Calculate mathematical statements for multiplication using repeated addition) and division within	Use an array to represent a teens number multiplied by a single digit number and partition the array into ten and ones to support calculating the product	number m numbe	oning to calculate a teens ultiplied by a single digit er (mental jotting or grid method)	Use known facts to m multiple of 10 by a sin number, e.g. 70 x 4 7 x 10 x 4 reorder 7 x 4 x 10	ngle digit = 280	Use partitioning to calculate a two- digit number multiplied by a single digit number using grid method	Write and calculate mathematical statements for multiplication and division using the multiplication tables
the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs	Use concrete materials to show di repeated subtraction for numbers b multiplication facts that they know, shown as 52 cubes put into grou	eyond the e.g. 52 ÷ 4	repeated subtraction for multiplication facts that multiples of the divisor, cubes put a group of 40	als to show division as or numbers beyond the they know using greater e.g. 52 ÷ 4 shown as 52 0 (10 groups of 4) and a ps of 4) so there are	repeated multiplicat multiples subtract	tical number line to show division as subtraction for numbers beyond the ion facts that they know using greater of the divisor e.g. 52 ÷ 4 shown as 52 ± 40 (10 groups of 4) leaves 12; then act 12 (3 groups of 4) so there are 13 groups of 4 in 52	that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
No equivalent objective in Year 2		Т	here are no steps towards	this end of year expectation	Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy		
Solve problems involving multiplication and division (including those with remainders), using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts			ent access to arrange of co ual Learning and Assessme				Solve problems, including missing number problems, involving multiplication and division (and interpreting remainders), including positive integer scaling problems and correspondence problems in which nobjects are connected to mobjects

	End of Year 2 expectation		Lea	arning and Progr	ression Stateme	nts			End of Year 3 expectation
	No equivalent objective in Year 2	(e.g. $\frac{3}{4}$ can e.g. demonstrate that three ap	on is one whole number divide be interpreted as 3 ÷ 4) oples shared (divided) betweer an apple for each child			(e.g. $\frac{3}{4}$ can be int	erpreted ures of o	bjects or fractional strips) that	Show practically or pictorially that a fraction is one whole number divided by another (e.g. $\frac{3}{4}$ can be interpreted as $3 \div 4$ )
	Recognise, find, name and write fractions $\frac{1}{3}$ , $\frac{1}{4}$ , $\frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity	(sharing) the amount equall amount equally	ow that you find $\frac{1}{2}$ of an amour y between two; $\frac{1}{3}$ is found by one, e.g. to find $\frac{1}{3}$ of 15 you divide into 3 equal groups	dividing the	Understand t	that finding a fraction of by the de e.g. to find $\frac{1}{4}$ of 12	nominat		Understand that finding a fraction of an amount relates to division
ractions	No equivalent objective in Year 2	Use concrete materials to show $\frac{1}{10}$ of an amount can be found dividing (sharing) the amount equally between ten.	number by 10 e.g. ex	a one-digit xchange each h straw piece changes and	place value o	che tenths heading in olumns represents a r of fractional tenths, is equal to 0.3	Describe the effect of dividing a one-digit number by ten, e.g. 7 ÷ 10 = 0.7 The 7 has moved one place to the right; from the ones column to the tenths column. A place holder (zero) is needed in the ones column		Recognise that tenths arise from dividing objects into 10 equal parts and in dividing one-digit numbers or quantities by 10
Number – Fractions	Recognise, find, name and write fractions $\frac{1}{3}$ , $\frac{1}{4}$ , $\frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity	Where a fraction of an amount cannot be found by using known division facts, use concrete materials to find unit fractions (with denominators of ten or less) of a set of objects, e.g. $\frac{1}{7}$ of 63	Use concrete materials to find non-unit fractions (with denominators of ten or less) of a set of objects, e.g. $\frac{3}{5}$ of 65	amount canno using known use pi representati model, to find	ctorial ions, e.g. bar I unit fractions If objects,	Use pictorial representations, e.g model, to find non-fractions of a set of c within multiplication knowledge, e.g. $\frac{3}{8}$ c	-unit objects o table	Use pictorial representations, e.g. bar model, to find non-unit fractions of a set of objects beyond multiplication table knowledge (using a multiplication grid), e.g. $\frac{3}{7}$ of 56	Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators
	Write simple fractions for example, $\frac{1}{2}$ of 6 = 3 and recognise the equivalence of $\frac{2}{4}$ and $\frac{1}{2}$	12		ow $\frac{2}{8}$ red, three	Use pictoria	ll representations such fractions ar		on walls to recognise where llent	Recognise and show, using diagrams, equivalent fractions with small denominators
	No equivalent objective in Year 2		, such as fraction strips, to add		Add and subtract fractions with the same denominator within one whole by adding or subtracting the numerators, e.g. $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$				Add and subtract fractions with the same denominator within one whole [for example, $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$ ]

No equivalent objective in Year 2	Use pictorial representations, such as fraction strips, to compare and order fractions with the same denominators	frac den	ompare and order ctions with the same cominator by placing cm on a number line	Use pi representati fraction strips and order u	ons, such as s, to compare	re the fraction; when the		Compare and order unit fractions such as $\frac{1}{3}$ , $\frac{1}{4}$ , $\frac{1}{2}$ , $\frac{1}{6}$ and $\frac{1}{2}$ by positioning them on a number line demarcated into twelve divisions	Compare and order unit fractions, and fractions with the same denominators (including on a number line)
Count on and back in steps of $\frac{1}{2}$ and $\frac{1}{4}$	Count on in steps of $\frac{1}{3}$ in the f $\frac{1}{3}$ , $\frac{2}{3}$ , $\frac{3}{3}$ , $\frac{4}{3}$ , $\frac{5}{3}$	form	Count back in steps of $\frac{5}{3}, \frac{4}{3}, \frac{3}{3}, \frac{2}{3}$	3		teps of $\frac{1}{3}$ in the form $\frac{1}{3}$ , $1\frac{2}{3}$ , $2\frac{1}{3}$ , $2\frac{2}{3}$ , $3$	back in steps of $\frac{1}{3}$ in the form $\frac{2}{3}$ , 2, $\frac{1}{3}$ , 2, 1, $\frac{1}{3}$ , 1, $\frac{1}{3}$ , 1, $\frac{2}{3}$ , $\frac{1}{3}$	Count on and back in steps of $\frac{1}{2}$ , $\frac{1}{4}$ and $\frac{1}{3}$	
No equivalent objective in Year 2			n need frequent access t lying, Contextual Learni	-	_				Solve problems that involve all of the above

	End of Year 2 expectation			Learning and Prog	ression Statements				End of Year 3 expectation
	Identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line. Identify	Accurately draw 2-D	shapes on dotty paper	(squared and isometric)		specific prope shape with exa		paper, e.g. draw a four- t angles	Draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes
	and describe the properties of 3-D shapes, including the number of edges, vertices and faces.		terials such as Clixi or ake 3-D shapes		3-D shapes using straws Playdoh		different o	cribe 3-D shapes in rientations, hapes has five faces?	in different orientations and describe them
Geometry – Properties of Shape	Distinguish between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anticlockwise)			nd identify objects in the the hands on a clock face	Recognise where sides meet at a vertex in a shape that an angle is created				Recognise angles as a property of shape or a description of a turn
Geometr	Distinguish between rotation as a turn and in terms of right angles for quarter, half and three-	tinguish between patation as a turn I in terms of right gles for quarter, half and three- quarter turns  Recognise a quarter- turn (as one right angle) from different starting points  Recognise a drawn right angle when presented in any orientation			Recognise a three- quarter-turn (as three right angles) from	four right a different sta and that th	Identify whether an angle is less than a right angles) from erent starting points d that the start and		Identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a
	(clockwise and anti-			be facing in opposite directions	different starting points		nts will be same	Identify whether an angle is greater than a right angle	complete turn; identify whether angles are greater than or less than a right angle
	No equivalent objective in Year 2		y vertical lines as lines that right angles to the horizon	Identify pairs of perpendicular line as lines that are at right angles to each other, or will be if they are continued, irrespective of orientation		are always the same distance apart irrespective of length (NB parallel lines can also be curved or concentric circles), irrespective		Identify horizontal and vertical lines and pairs of perpendicular and parallel lines	

Geometry – Position and Direction	End of Year 2 expectation	Learning and Progression Statements			
	No equivalent objective in Year 2	Know that squares in the same vertical column will all have the same letter reference (but a different number reference), e.g. A3 and A5			
		Know that squares in the same horizontal row will all have the same number reference (but a different letter reference), e.g. B2 and D2	with letters and numbers		

Statistics	End of Year 2 expectation	Learning and Progression Statements						End of Year 3 expectation			
	Compare and sort numbers and common 2-D and 3-D shapes and everyday objects	objects, numbers and shapes including items that		e Venn diagrams with two non-intersecting sets compare and sort objects, numbers and shapes including items that do not fit the criteria and placing these in the universal set (area outside the circles)  Use Venn diagrams with two intersecting sets to compare and sort objects, numbers and shapes including items that do not fit the criteria and placing these in the universal set (area outside the circles)			Use sorting diagrams to compare and sort objects, numbers and				
		Use one criterion Carroll diagrams to compare and sort objects, numbers and shapes  Use two criteria Carroll diagrams to compare and sort objects, numbers and shapes (understanding that Carroll diagrams are labelled 'is' and 'is not')					common 2-D and 3-D shapes				
	Interpret and construct simple pictograms, tally charts, block diagrams and simple tables	Interpret and present data using bar charts with a scale in ones	Interpret and pres using bar charts wit in twos		using bar char	l present data ts with a scale ives		et and present data r charts with a scale in tens	Select the most appropriate scale when representing data in a bar chart or pictogram	Interpret and present data using bar charts,	
		Interpret and present data using tables						pictograms and tables			
	Ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity.  Ask and answer questions about totalling and comparing categorical data	Use and interpret information in scaled bar charts and pictograms and tables to solve one-step questions such as 'How many more?' and 'How many fewer?'			to solve two- categories	step questi to compare	ons such as those inv	— ·	Solve one-step and two-step questions [for example, 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables		

	End of Year 2 expectation	Learning and Progression Statements									
	Choose and use appropriate standard units to estimate and measure length/height in any direction	Measure lengths (m/cm/mm)  Compare the lengths of different objects		Add values of length (m/cm/mm) (see progression in mental and written addition)	expectation						
Measurement	(m/cm); mass (kg/g); temperature (°C); capacity and volume (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels. Compare and order lengths, mass, volume/capacity and record the results using >, < and =	Measure mass (kg/g)	Compare the mass of different objects	Add values of mass (kg/g) (see progression in mental and written addition)	Find the difference between the masses of objects and say by how much an object is heavier or lighter (kg/g)  (see progression in mental and written subtraction)	Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (I/mI)					
		Measure volume/capacity (I/mI)	Compare the volume/capacity of different objects	Add values of volume/capacity (I/mI) (see progression in mental and written addition)	Find the difference between the volumes/capacities of vessels and say how much more or how much less one vessel contains than another (I/mI)  (see progression in mental and written subtraction)						
Mea	Estimate and measure temperature to the nearest degree (°C) using thermometers	There are no steps towards this end of year expectation									
	No equivalent objective in Year 2	Use concrete materials, e.g. straws, to create a 2-D shape; deconstruct the straws into a straight line to show that the perimeter is a measure of length around the boundary									
	No equivalent objective in Year 2	wheel to measure large polygons dra the lengths of the sides are in whole	er of a polygon, either using a trundle wn in chalk on the playground where metres, or shapes drawn on squared cre paper	Measure the perimeter of simple pol ruler and calcu	Measure the perimeter of simple 2-D shapes						
	Tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times	Tell and write the time on an analogue clock to the nearest minute for times past the hour, e.g. 12 minutes past 2	Tell and write the time on an analogue clock to the nearest minute for times to the hour, e.g. 22 minutes to 4	Know that when reading and writing the time on a digital clock, the hours and minutes are separated by a colon	Tell the time on a digital clock to the nearest minute and know whether this is before or after midday, e.g. 4:27 am is 27 minutes past 4 in the morning	Tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks					

Tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times		f reference for time such as for teeth brushing is 2 minu for six hours		Use the common points of reference they know to estimate the time of various events			Estimate/read time with increasing accuracy to the nearest minute	
No equivalent		Use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon, midnight						
objective in Year 2	sandwich in	ervals which are in the same 42 seconds, my friend took no ate their sandwich quick	56 seconds.	Record time in terms of seconds, minutes, hours			vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon, midnight	
Know the number	Know that there are 60 seconds in a minute							
of minutes in an hour and the number of hours in	Know the number of days in each month							
a day	Know that there are 365 days in a year but 366 in a leap year; know that a leap year occurs every 4 years when the year is divisible by 4							
Compare and sequence intervals of time	Solve time problems working within the hour boundary, e.g. It is 10:30am. My favourite programme starts at 10:45am. How many minutes until it starts?	Solve time problems that involve the start time and duration where the end time is to be calculated, (within the hour) e.g. a cake goes in the oven at 3:20. It needs to bake for 30 minutes. At what time do I need to take it out of the oven?	Solve time problems that involve the end time and duration where the start time is to be calculated, (within the hour) e.g. it takes me 25 minutes to walk to school. I arrive at school at 8:50, what time did I set off?	Solve time problems working across the hour boundary, e.g. It is 3:45pm. How many minutes to 4:15pm?	Solve time problems that involve the start time and duration where the end time is to be calculated, (beyond the hour) e.g. Mike went on a 45 minute bike ride. He set off at 2:40. At what time did he finish?	Solve time problems that involve the end time and duration where the start time is to be calculated, (beyond the hour) e.g. my music lesson is 45 minutes long. It finished at 3:20, what time did it start	Compare durations of events [for example to calculate the time taken by particular events or tasks]	
Recognise and use symbols for pounds (£) and pence (p)	cognise and use abols for pounds  Recognise that pence is a fraction of a whole pound.		Recognise that when writing amounts of money, either £ or p are used but never together		Recognise that when an amount of money is in pounds and pence it can be written with a £ sign and a decimal point separating the whole pounds and the pence		Continue to recognise and use the symbols for pounds (£) and pence (p) and understand that the decimal point separates pounds/pence	

Combine amounts to make a particular value Find different combinations of coins that equal the same amounts of money			Recognise that each 10 which is consist	Recognise that ten 10p coins equal £1 and that each coin is $\frac{1}{10} \text{ of £1}$	
Solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change	Solve a one-step problem that involves adding two amounts of money, e.g. a television costs £240 and a games console costs £225.  What is the total cost?	Solve a one-step problem that involves subtractin an amount of money, e.g. John buys an apple for 37p. He pays with a £1 coin. How much change does he get?		buys a comic for £1.50 and puppet for £4.30. He pays with a £10 note.	
Solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change and measures (including time)	in a intext dition tion of e same ding ge and ge and ges				